Firms’ Heterogeneity in Capital/Labor Ratios and Wage Inequality

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Abstract

This paper provides some empirical evidence and a theory of the relationship between residual wage inequality and the increasing dispersion of capital/labor ratios across firms. I document the increasing variance of capital/labor ratios across firms in the US labor market. I also show that the increase in the variance of capital/labor ratios across firms is related to the increasing variance of wages across workers. To explain these empirical regularities I adopt a search model where firms differ in their optimal composition of capital between equipment and structure. As the relative price of equipment falls over time the distribution of capital/labor ratios becomes more dispersed across firms. In a frictional labor market this force generates wage dispersion among identical workers. Simple calibration of the model indicates that the dispersion of capital/labor ratios can explain up to one half of the total increase in residual wage inequality.

Keywords: Wage inequality, Capital intensity, Search models.
JEL classification: J21, J31.

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1 Introduction

Changes in wage inequality reflect changes in both price and quantities of workers' observable characteristics and changes in residual wage inequality. Juhn, Murphy and Pierce (1993) claim that roughly 60% of the increase in the 90-10 log wage differential can be accounted by changes in the residuals' distribution, i.e. in unobserved attributes of workers belonging to the same demographic or educational group.

While there are already many studies on increasing wage dispersion, much less research has been devoted to the increasing dispersion of capital intensity across firms. This paper is articulated in three parts. The first part is an analysis of dispersion of equipment/labor ratios across firms. The second part provides some empirical evidence of the link between the dispersion of wages across workers and the dispersion of capital intensity across firms. In the third part of the paper, I propose a theory of residual wage inequality based on the increased dispersion of capital intensities across firms.

In the first part of this paper I use panel data on individual firms (Compustat) from 1970 to 1992 to document the increase over time of the variance of equipment/labor ratios. I focus on equipment capital as equipment is complementary to skills and differential stocks of equipment capital across firms may be correlated with the demand for skills. The results show that the log standard deviation across firms of equipment/labor ratios increased by about 12% from 1970 to 1992. The rise in dispersion of equipment/capital occurred both between and within industry and it is concentrated in the mid-late eighties.

In the second part of the paper, I study the correlation between the increasing dispersion of wages across workers and the increasing dispersion of capital intensities across firms. The data on wages are from March CPS and five waves of the Displaced Workers Survey (DWS). The reason to study displaced workers is twofold. First in the DWS there is a panel dimension that allows one to control for unobserved heterogeneity, secondly displaced workers are less likely to select themselves in the best paying industries or firms. This implies that the capital intensity premium is more likely to reflect "true" firms' effects rather than sorting. I match Compustat data on firms' capital intensity to CPS and DWS data on wages at the industry-year level. The results indicate that a 1% increase in the average industry capital intensity is associated to a 0.11% increase in the average weekly wage in the CPS and to a 0.13% increase in the DWS. Consistently with the literature on inter-industry wage differentials, there is no increase over time in the cross-industry effect of capital intensity on wages. More importantly for the
scope of this paper, within industry dispersion of equipment/labor ratios appears to be related to within industry dispersion of wages both in the CPS and in the DWS. Both the variance of equipment/labor ratios across firms and the variance of wages across workers have increased over time. The association between the dispersion of equipment/labor ratios across firms and the dispersion of wages across workers holds within industry even after controlling for time dummies.

In the theory part I build a model that explains the rise in the variance of wages in view of the evidence on the increasing variance across firms of the equipment/labor ratios. The intuitive idea is simple. The two main ingredients of the model are non competitive labor market and random matching of identical workers to two types of firms. In a non competitive labor market workers' wages are linked to their individual output and therefore to the capital they are matched with. Identical workers are matched randomly to two types of firms that co-exist in equilibrium. "Good" firms invest little in structure and a lot in equipment, "bad" firms do the reverse. As the relative price of equipment capital falls, "good" firms with a high ratio equipment/structure invest more and increase their productivity relative to "bad" firms. Wages for identical workers are more dispersed as a consequence of a higher dispersion of capital intensities. This feature of the model that explains the increase of wage inequality with increasing dispersion of capital intensities across firms is consistent with recent evidence that indicates that the bulk of the increase in wage inequality took place between plants rather than within plants (Dunne et al. 2002).

1.1 A Brief Overview of the Related Literature

Work on dispersion of capital/labor ratios is fairly rare in the literature. Caselli (1999) uses industry-level data to document the increase in the 90-10 log differential of capital intensities across four-digit manufacturing industries. In this paper I use data on individual firms to study the increasing dispersion of equipment/labor ratios across firms.

The empirical part of this paper is connected to the literature that exploits establishment-level data to study the dispersion of wages and productivity across plants. Davis and Haltiwanger (1991) and Dunne et al. (2002) show that the increase in wage dispersion is mainly a between-plant phenomenon. Using both individual wage data and establishment-level data they decompose the total variance of wages in three components: between-industry, between-plant and within-plant. The results show that most of the increase in wage dispersion can be accounted by between-plant dispersion.
within the same industries. Related work by Doms et al. (1997) finds that an important factor in explaining wage dispersion across plants is the differential adoption of technologies. Dunne et al. (2002) find that between-plant measures of wage and productivity dispersion have increased over time and are strongly positively correlated. They also find that a significant fraction of the rising dispersion of wages and productivity is associated with changes in the distribution of computer investment across plants.

Unlike with wages and computers, however, there has been little analysis of the changes in the distribution of capital intensity over time and of the association between wages and capital intensity. All previously cited papers use establishment-level data limited to manufacturing. In this paper I use Compustat data to study the evolution of the distribution of capital intensity over time across firms in all industries.

In the theory part, I propose a model of residual wage inequality based on the increased dispersion of capital intensities across firms. There are many theories of within-group wage inequality built on the complementarity between unobservable skills and new technologies. Most models, however, interpret unobservable skills as ex ante differences in ability across individuals. The model of residual wage inequality presented here is not based on ex ante differences in unobservable ability. In this model identical workers are matched to different firms. The mainstream view in the literature is that within group wage inequality is the result of the increase in the price of unobserved ability. Acemoglu (1999) builds a model where identical firms search for workers with different abilities. Skill biased technical change induces firms to switch from a pooling equilibrium where one job fits for all, to a separating equilibrium where different jobs for different abilities are created. Caselli (1999) suggests that a technological revolution occurs with the introduction of a new type of machine. Operating the new machine requires a new type of skill. Workers have different costs of learning the new skill and those with lower learning costs can get a higher wage premium. Galor and Moav (2000) claim that ability helps to adapt to the new work organization, therefore big organizational changes raise the return to ability. Kremer and Maskin (2000) build a model where production requires many complementary tasks. Wage inequality increases as workers with different skills are increasingly segregated across plants. Segregation occurs because of the complementarity of

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1 Although in the published version Dunne at al. (2002) focus on the relationship between wage and computer investment across plants, in the Working Paper version, they also study the relationship between capital intensity and wages.
tasks and the exogenous force that sets the mechanism in motion is the increasingly dispersed distribution of skills across workers.

All these models provide explanations through which technology might affect inequality, however, they are all based on ex-ante differences in ability. Models based on fixed ex-ante differences in ability are subject to an important criticism. Unobserved ability is a permanent characteristic of the individual therefore all models based on differences in innate ability imply that the rise in residual wage inequality should be accounted for by the rise in the variance of the persistent component of individual earnings. Gottschalk and Moffitt (1994, 1995) and the subsequent literature show that this is not the case and earnings’ instability (the variance of the transitory component) explains much of the total increase.

On the basis of this criticism Violante (2002) proposes a model based on ex-ante identical workers where wage inequality is due to an acceleration of technical change and transferability of skills across jobs. In each period a new vintage technology embodied in new machines diffuses in the economy. Workers are ex-ante identical and have vintage specific skills. The degree of transferability of these skills between different vintages is proportional to the productivity difference between the machines. An acceleration in technical change increases the productivity differences across successive vintages and decreases the degree of transferability of skills. As a result wage inequality across identical workers matched to different vintages of machines rises.

The models of Acemoglu (1999), Caselli (1999) and Violante (2002) are all consistent with an increasingly dispersed distribution of capital intensity. My model is built around an increasingly dispersed distribution of capital intensity. Like Violante (2002), my model does not rely on ex ante differences in abilities. Differently from Violante (2002), my model is not based on a technological acceleration and the reduction in the transferability of skills. In my model, a decrease in the relative price of equipment capital rises wage inequality increasing the dispersion of capital intensities across firms.

The model presented in this paper is related to the literature that explains wage dispersion among equivalent workers with differences in firms’ technology. Some of these models as Montgomery (1991), Acemoglu (2000) and Pissarides (1994) consider firms with different technologies and derive wage dispersion as a consequence of technology dispersion. My model is closest to Acemoglu (2000). He also considers a search model with different technologies across firms but he focuses on the effect of more generous unemployment insurance and minimum wage on the composition of jobs.

Finally, an increasingly dispersed distribution of equipment/labor ratios can have an effect on wage differentials across identical workers as long as the
market is not competitive and firm effects are important in determining the wage. This paper is therefore related to the literature on inter-industry wage differentials. There is a controversy on the importance of unobserved person or firm effects in explaining inter-industry wage differentials. Krueger and Summers (1988) and Gibbons and Katz (1992) claim that the differentials cannot be explained by person effects. Murphy and Topel (1990) claim that person effects are the primary explanation. Abowd, Kramarz and Margolis (1999) using employer-employee matched dataset estimate that person and firms effects can account each for approximately 50% of the inter-industry wage differentials.

The structure of the paper is as follows. In the next section I document the increase in the variance of capital/labor ratios between and within industry over time. In section 3, I relate the variance of wages to the variance of capital/labor ratios. In section 4, I present the model that interprets the evidence. Section 5 concludes.
2 Firms Equipment/Labor Ratios

In this section I examine changes over time in the cross-firm distribution of capital/labor ratios. I use Compustat data from 1970 to 1992. Compustat is a dataset of US companies listed on the stock market. They represent less than 1% of the total number of companies in the US but more than 50% of total employment. Figure 1 plots the employment weighted standard deviation of log equipment/labor across firms in each year. To build the equipment/labor ratio I use information on equipment (COMPSTAT 156) and on the number of employees (COMPUSTAT 129). Equipment represents the capitalized cost of machinery and equipment used to generate revenue minus accumulated depreciation. Equipment is deflated using the 1-digit industry specific deflators form the Bureau of Economic Analysis.

Figure 1 shows an increase in the employment weighted standard deviation of log equipment/labor ratios across firms of 12.3% between 1970 and 1992. The increase in dispersion of equipment/labor ratios starts in 1980 and continues through the 80s. This paper is concerned with the increasing dispersion of equipment/labor ratios facing workers, hence the log standard deviation of equipment/labor ratios is employment-weighted.

Figure 2 shows that the divergence in equipment/labor ratios is pervasive and not limited to part of the distribution. Figure 2 gives the percentage change in equipment/labor ratios from 1970-73 to 1989-92. The changes are calculated considering the same percentile of the distribution in 1989-92 and in 1970-73. The change in real equipment/labor ratios at the bottom 10th percentile of the distribution is 55%, at the top 90th percentile of the distribution is 103%. The picture exhibits a concave shape with inequality rising more at the bottom 50% of the distribution.

The four panels in figure 3 decompose the rise in equipment/labor dispersion in four periods. I look at changes between periods of five years each. The first panel compares log equipment/labor ratios by percentile between the periods 1970-74 and 1975-79. The changes at each percentile are normalized by comparing the change at each percentile with the change in mean log equipment/labor ratios. The four panels show that from 1970-74 to 1975-79 and from 1980-83 to 1984-88 equipment/labor ratios at each percentile moved more or less in line with the mean. The increase in dispersion of equipment/labor ratios across firms took place in the early and in the late eighties, as the top right and bottom right panel in figure 3 show. The

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2 The results don’t change if I exclude from the sample the new firms that get in the sample after 1974.
increase in dispersion is concentrated at the bottom of the distribution in the early eighties (top right panel) with the bottom percentiles left much behind relative to the mean. The increase in dispersion paused somewhat in the mid eighties (bottom left panel) but continued from the mid eighties to the nineties (bottom right panel). In the late eighties (bottom right panel) the bottom percentiles grew about 10% less than the overall mean, the top percentiles grew about 10% more than the mean.

### 2.1 Between and Within Industry Dispersion

In this subsection I look at the increase in the dispersion of equipment/labor ratios between and within industry and size groups.

Table 1 and 2 report log equipment/labor differentials across industry and across size class. Table 1 and 2 report the mean capital intensity (column one), the within group standard deviation (column two) and the frequency in the sample (column three). The mean log equipment/labor differentials by industry and size group (first column Table 1 and 2) are defined as the difference between the average log equipment/labor ratio within the group and the overall average log equipment/labor ratio. Table 1 reports time
Figure 3: Changes in relative real equipment/labor $\frac{e}{l}$ ratio. Four periods $t$. In figure $[p_t(\log \frac{e}{l}) - p_{t-1}(\log \frac{e}{l})] - [E_t(\log \frac{e}{l}) - E_{t-1}(\log \frac{e}{l})]$ where $p$ is the percentile of the employment weighted log distribution in period $t$. $E$ is the employment weighted average.
series averages and table 2 reports time series changes between 1970-73 and 1989-92. I consider groups of three years to minimize measurement error.

The sectors with the higher average equipment/labor ratios (table 1, column one) are agriculture and mining, transportation and utilities, and finance. These three sectors have much higher equipment/labor ratios than the overall mean. The lower capital intensive industries are wholesale and retail and business and professional services. The heterogeneity of log equipment/labor ratios across firms of the same industry (table 1, column two) is also higher within agriculture and mining, transportation and utilities, and finance. Equipment/labor ratios are higher at small companies with less than 100 workers and at very large companies with more than 4000 workers. The differences across size groups are less impressive than the differences across industry groups. Differences are larger between small firms and medium-sized firms. Firms of small size are more heterogeneous in their equipment/labor ratios than firms of large size. The heterogeneity of equipment/labor ratios within size classes is decreasing with size.

Looking at the time series changes in table 2, the average equipment/labor ratio (table 2, column one) within agriculture, transportation, retail, finance and business and professional services increased less than the overall average between 1970 and 1992. Manufacturing and construction gained ground relative to the mean. Between firm equipment/labor dispersion (table 2, column two) rose in all sectors except for transportation and personal and business services. The highest increases occurred in manufacturing, retail trade and finance. The differentials in equipment/labor ratios across size classes increased dramatically over time. The difference between firms of less than 100 workers and firms of more than 4000 workers increased by 50% between 1970 and 1992. Between firm dispersion in equipment/labor ratios increased within all size classes except for companies below 100 workers. Small firms below 100 workers became relatively less capital intensive over time and much more homogenous.

Finally the last column of table 2 indicates a sizeable shift out of manufacturing and into business and professional services and a shift from large firms of more than 1000 workers into smaller firms.
### Table 1: Time series averages

<table>
<thead>
<tr>
<th>Industry</th>
<th>Mean log equipment/labor differential</th>
<th>Between firm standard deviation</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>Agriculture/mining</td>
<td>0.79</td>
<td>1.29</td>
<td>1.81</td>
</tr>
<tr>
<td>Construction</td>
<td>-0.10</td>
<td>1.02</td>
<td>1.45</td>
</tr>
<tr>
<td>Manufacturing</td>
<td>0.05</td>
<td>0.99</td>
<td>59.48</td>
</tr>
<tr>
<td>Transportation/utilities</td>
<td>0.66</td>
<td>1.35</td>
<td>7.96</td>
</tr>
<tr>
<td>Wholesale/retail</td>
<td>-0.54</td>
<td>0.86</td>
<td>13.36</td>
</tr>
<tr>
<td>Finance</td>
<td>0.08</td>
<td>1.82</td>
<td>3.58</td>
</tr>
<tr>
<td>Other services</td>
<td>-0.44</td>
<td>1.04</td>
<td>13.06</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Size class</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1-100 employees</td>
<td>0.11</td>
<td>1.30</td>
<td>14.3</td>
</tr>
<tr>
<td>100-500</td>
<td>-0.03</td>
<td>1.12</td>
<td>23.3</td>
</tr>
<tr>
<td>500-1000</td>
<td>-0.01</td>
<td>1.09</td>
<td>13.1</td>
</tr>
<tr>
<td>1000-4000</td>
<td>-0.07</td>
<td>1.07</td>
<td>24.9</td>
</tr>
<tr>
<td>4000+</td>
<td>0.04</td>
<td>1.03</td>
<td>24.2</td>
</tr>
</tbody>
</table>

Notes: Time series averages. Mean log equipment/labor differentials and between firm dispersion by industry and size groups.

### Table 2: Time series changes 1970-1992

<table>
<thead>
<tr>
<th>Industry</th>
<th>Mean log equipment/labor differential</th>
<th>Between firm standard deviation</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>Agriculture/mining</td>
<td>-0.09</td>
<td>0.08</td>
<td>0.00</td>
</tr>
<tr>
<td>Construction</td>
<td>0.19</td>
<td>0.01</td>
<td>-0.00</td>
</tr>
<tr>
<td>Manufacturing</td>
<td>0.14</td>
<td>0.19</td>
<td>-0.12</td>
</tr>
<tr>
<td>Transportation/utilities</td>
<td>-0.17</td>
<td>-0.03</td>
<td>0.05</td>
</tr>
<tr>
<td>Wholesale/retail</td>
<td>-0.21</td>
<td>0.22</td>
<td>-0.02</td>
</tr>
<tr>
<td>Finance</td>
<td>-0.05</td>
<td>0.19</td>
<td>0.00</td>
</tr>
<tr>
<td>Other services</td>
<td>-0.03</td>
<td>-0.07</td>
<td>0.09</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Size class</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1-100 employees</td>
<td>-0.49</td>
<td>-0.22</td>
<td>0.14</td>
</tr>
<tr>
<td>100-500</td>
<td>-0.08</td>
<td>0.09</td>
<td>0.09</td>
</tr>
<tr>
<td>500-1000</td>
<td>0.04</td>
<td>0.22</td>
<td>-0.02</td>
</tr>
<tr>
<td>1000-4000</td>
<td>0.05</td>
<td>0.29</td>
<td>-0.11</td>
</tr>
<tr>
<td>4000+</td>
<td>0.01</td>
<td>0.25</td>
<td>-0.09</td>
</tr>
</tbody>
</table>

Notes: Time series changes between 1970-73 and 1989-92. Changes in log equipment/labor relative to the mean log change and changes in between firm dispersion by industry and size groups.

### 2.2 The Juhn Murphy and Pierce Decomposition

To characterize the contribution of observable and unobservable characteristics to the changes in the equipment/labor distribution over time, I use the distribution accounting methodology of Juhn, Murphy and Pierce (JMP). The observable characteristics I consider are industry and size.
Consider the regression:

$$\log k_{it} = X_{it}\beta_t + u_{it}$$

(1)

where $$\log k_{it}$$ is log equipment/labor ratio in firm $$i$$ in period $$t$$. $$X_{it}$$ is a vector of observable characteristics which contains 2-digit industries dummies and a quartic in size (number of employees). $$\beta_t$$ is the vector of OLS estimated equipment/labor differentials and $$u_{it}$$ is the residual which reflects price and quantities of unobserved firm characteristics and it is independent of $$X_{it}$$.

Define $$\vartheta_{it}$$ as the percentile in the distribution function of the residuals in year $$t$$: $$\vartheta_{it} = F_t(u_{it})$$. Therefore $$u_{it}$$ can be written: $$u_{it} = F_t^{-1}(\vartheta_{it})$$. To isolate the contribution of changes in industry and size composition consider:

$$\log k_{1it} = X_{it}\bar{\beta} + F^{-1}_t(\vartheta_{it})$$

where $$\bar{\beta}$$ is the average equipment/labor differential calculated over the whole period. $$F^{-1}_t(\cdot)$$ is the average inverse cumulative distribution of residuals. The time path of the distribution over $$\log k_{1it}$$ represents an estimate of the effect of the changes in the distribution of observable characteristics $$X_{it}$$ on the distribution of equipment/labor ratios. To calculate the marginal contribution of changes in inter-industry and size specific equipment/labor differentials consider:

$$\log k_{2it} = X_{it}\beta_t + F^{-1}_t(\vartheta_{it})$$

Calculating the distributions $$\log k_{it}$$, $$\log k_{1it}$$, and $$\log k_{2it}$$ for each year in the sample, we can attribute the changes in $$\log k_{1it}$$ to changes in industry and size composition, the changes in $$\log k_{2it} - \log k_{1it}$$ to changes in inter-industry and size specific equipment/labor differentials and the changes in $$\log k_{it} - \log k_{2it}$$ to changes in the distribution of residuals.

The top left panel of figure 4 plots the time series of the differential between the 90th and the 10th percentile of the employment-weighted log distribution of equipment/labor ratios, $$\log k_{it}$$. The other three panels of figure 4 break down the growth in the 90-10 differential into the three components of the JMP decomposition. Each component is measured as a deviation from its own overall mean. The top right panel gives the effect of the changes in the distribution of the observables. Changes in observable characteristics started to contribute positively to the increase in equipment/labor dispersion in the 1980s. During the 70s the industrial and size composition of firms worked towards a reduction of the overall inequality in equipment/labor.

ratios. The bottom left panel of figure 4 looks at the effect of the changing industry and size differentials, keeping the composition of the sample constant. The bottom right panel of picture 4 indicates that the effect of unobservables is particularly concentrated in the 1970s rather than in the 80s.

The results from figure 4 are reported in table 3. The 90-10 log differential rose from 2.46 in 1970 to 2.78 in 1992 (or 13%). Changes in industrial and size composition over twenty years (holding fixed the equipment/labor differential associated with industry and size) contributed to 28% (0.09/0.32) of the total increase in the 90-10 log differential. Changes in the industry and size differentials alone (holding fixed the industry and size composition) contributed to 6% (0.02/0.32) of the total increase of the 90-10 log differential. Changes in composition and differentials together account for 34% of the total increase of the 90-10 differential. The remaining 66% of the total increase of the 90-10 differential is explained by unobservables, i.e. by the rise in within industry-size groups dispersion.

<table>
<thead>
<tr>
<th>Inequality measure</th>
<th>Total change</th>
<th>Observable quantities</th>
<th>Observable betas</th>
<th>Unobservables</th>
</tr>
</thead>
<tbody>
<tr>
<td>Standard deviation</td>
<td>0.12</td>
<td>0.08</td>
<td>0.00</td>
<td>0.04</td>
</tr>
<tr>
<td>90-10 differential</td>
<td>0.32</td>
<td>0.09</td>
<td>0.02</td>
<td>0.21</td>
</tr>
<tr>
<td>90-50 differential</td>
<td>0.18</td>
<td>-0.01</td>
<td>-0.01</td>
<td>0.20</td>
</tr>
<tr>
<td>50-10 differential</td>
<td>0.13</td>
<td>0.09</td>
<td>0.02</td>
<td>0.02</td>
</tr>
</tbody>
</table>

Notes: Juhn, Murphy and Pierce decomposition. The regression specification underlying the decomposition contains 2-digit industry effects and a quartic in size.

The JMP decomposition can be used to quantify the effects of changes in the observables and the unobservables on all parts of the distribution. Table 3 reports the decomposition of time series changes in the 90-50 and 50-10 log equipment/labor differentials. Two important results stand out from the table. First, most of the increase in equipment/labor dispersion occurred in the top half of the distribution. Secondly, the contribution of observables to the increase in equipment/labor ratios across firms varies according to the inequality measure reported. The increase in between size and industry group inequality accounts for approximately three quarters of the total increase in the standard deviation of equipment/labor ratios. The increase in between group inequality accounts for 84% of the increase in the 50-10 ratio but doesn’t explain at all the increase in the 90-50 ratio. Apparently the capital intensity gap between the 50th percentile of the distribution and the 10th percentile is much more understandable in terms of changes in industrial and size composition and differentials than the gap between the 90th and the 50th percentile.

3 The Variance of Capital/Labor Ratios and Wage Inequality

In this section I document the cross-industry correlation between firms’ equipment/labor ratios and wages from 1970 to 1992. First I study the correlation between wages and average industry capital intensity, secondly I look at the correlation between within industry dispersion of wages and within industry dispersion of capital/labor ratios.

The tendency of capital intensive industries to pay higher wages has been documented by Katz and Summers (1989) in the context of inter-industry wage differentials. The correlation between within industry dispersion of
wages and within industry dispersion of capital intensities is a novel point.\textsuperscript{3} Differently from previous work I study the relationship between individual wages and the average industry’s capital intensity over time. I match individual wages drawn from March CPS to average capital intensity at the industry-year level drawn from Compustat. I also extend the analysis to displaced workers. Displaced workers have been extensively used in the literature on inter-industry wage differentials.\textsuperscript{4} The idea is that an exogenous displacement reduces the problem of sorting of better workers into better paying industries and gives a better measure of the pure industry effect. Following the same reasoning, I investigate whether an increasing dispersion of wages for displaced workers is associated with an increasing dispersion of capital intensity across firms.

Figure 5 shows the log standard deviation of weekly wages and the employment-weighted log standard deviation of equipment/labor ratios. Log equipment/labor ratios are drawn from Compustat, log weekly wages are from March CPS. In the following section I investigate the relationship formally.

### 3.1 The "Capital Intensity" Premium

I regress log weekly wages from March CPS on industry employment-weighted average log equipment/labor ratios from Compustat. The two datasets are matched at the one-digit industry-year level.

I restrict the March CPS sample to full year, full time workers (those working 35 or more hours per week and at least 40 weeks in the previous year) between the age of 20 and 60 at the time of the survey. I use March CPS data from 1971 to 1993 therefore covering earnings from 1970 to 1992. The sample is restricted to workers without allocated earnings, who earned at least $67 per week in 1982 dollars.\textsuperscript{5}

The regression is of the form:

$$\log w_{ijt} = \alpha + X_{it} \beta + \gamma \log(\frac{k}{l})_{jt} + \epsilon_{ijt}$$  \hspace{1cm} (2)

where $\log w_{ijt}$ is the wage of individual $i$ at time $t$ in industry $j$. $X_{it}$ includes year and industry effects, a quadratic in age, years of education, sex,

\textsuperscript{3}The working paper version of Dunne et al.(2002) contains some analysis of the correlation between wages and capital intensities over time in a panel of manufacturing firms.

\textsuperscript{4}Krueger and Summers (1988), Gibbons and Katz (1992) and Neal (1995) have used the Displaced Workers Survey to study interindustry wage differentials.

\textsuperscript{5}This selection of the March CPS is used in Katz and Autor (1999).
Figure 5: Log standard deviation of real weekly wages from March CPS. Employment-weighted log standard deviation of equipment/labor ratios from Compustat. CPI prices and 1-digit industry specific capital deflators at 1992 values

race and marital status dummies. \( \log(\frac{\mathcal{E}}{W})_{jt} \) is the employment-weighted average equipment/labor ratio in industry \( j \) at time \( t \). Standard errors are clustered at the industry-year level. I consider the following industries: durable manufacturing, non-durable manufacturing, transport and utilities, wholesale trade, retail trade, and other services. Agriculture, mining and construction are dropped because of the low sample size of the year cells in Compustat. Workers in public administration are dropped as Compustat data on capital intensity cover only the private sector. Wages are deflated by the CPI, equipment is deflated using 1-digit industry specific deflators from the Bureau of Economic Analysis.

Table 4 shows the results of OLS estimation of equation 2 separately for the CPS and the DWS. The results show a positive relationship between average industry’s capital intensity and weekly wages. The first row of table 4 shows that a 1% increase in the industry capital intensity is associated with a 0.11% increase in the average weekly wage. The relationship between wages and capital intensity controlling for year effects is always positive and significant. This is the familiar result that more capital intensive industries tend to pay higher wages. Equipment capital intensity and average wages are mildly negatively correlated within industry (table 4, first and second
row and third column), and their correlation is insignificant when I control for both industry and time effects (table 4, fourth column). This result is consistent with the view that inter-industry wage differentials have not increased over time. The same results are obtained in the second row of table 4 considering the years 1984-1992 of the CPS. This sample’s cut is used to compare the results with the Displaced Workers Survey.

3.2 The Displaced Workers Survey

In this section I estimate equation 2 using the Displaced Workers Surveys in years 1984, 1986, 1988, 1990 and 1992. The Displaced Workers Survey is a supplement to the January CPS in years 1984, 1986, 1988, 1990, 1992. The DWS asks whether the workers were displaced in the five years prior to the survey. It contains information about the previous and the current wage, industry and occupation and information about a respondent’s employment history in the previous 5 years.

The use of the DWS has two advantages: First the DWS has a panel dimension that allows one to control for unobserved heterogeneity; secondly displaced workers are less likely to select themselves in the most capital intensive industry and within industry in the most capital intensive firms. As a result the coefficient on industry capital intensity are more likely to reflect true firms’ effect rather than sorting. The thought experiment that motivates this analysis is the following: imagine a group of workers is exogenously displaced and then randomly assigned to a new firm, either within the same industry or in a different industry. Given the big increase in the dispersion of capital/labor ratios across firms, we expect to see a positive relationship between the variance of the wages and the variance of capital intensity within and between industry.

I restrict the sample to workers who are employed full time in both the pre-displacement and current job. This restriction is necessary as the wage information is in terms of weekly wages. The sample is further restricted to workers aged 20-60 at the time of the survey. The reasons for displacement can be various, in the following tables I present the results on the whole sample of displaced workers, the results obtained on the subsample of the displaced because of establishment closings are qualitatively similar.

The results of estimation of equation 2 on DWS data are shown in table 4, row three. The results are similar to those obtained on CPS data. In the pooled sample (row three, first column), a 1% increase in equipment capital intensity implies a 0.13% increase in the average wage post-displacement. Wages and capital intensity are positively associated across industries (row
three, second column), but are not associated within industry (row three, third column). Controlling for both industry and year effects, (row three, fourth column), capital intensity and wages are not significantly associated.

The same pattern holds when the regressions are run using fixed effect estimates. In this case both the information on wages pre and post-displacement is used and the average industry capital intensity in the pre-displacement job is matched according to the relevant year and industry. Table 4, fourth row, reports the results of the fixed effect estimation. A 1% increase in the change in capital intensity is associated to a 0.06% increase in the weekly wage change (difference between post-displacement wage and pre-displacement wage). The correlation between capital intensity changes and wage changes disappear when we control for both industry and time effects. All the regressions run with fixed effects include dummies to control for the years since displacement (25 dummies: years since displacement go from one to five for each of the five survey years). The regressions also control for the change of industry pre and post-displacement (36 dummies: six industries pre-displacement combined with six industries after displacement).

OLS estimates of the impact of average industry log equipment/labor ratio on log earnings.

<table>
<thead>
<tr>
<th>Dependent variable: Log weekly earnings</th>
<th>N obs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>CPS 1970–1992</td>
<td>603483</td>
</tr>
<tr>
<td>CPS 1984–1992</td>
<td>226497</td>
</tr>
<tr>
<td>DWS 1984–1992</td>
<td>8629</td>
</tr>
<tr>
<td>DWS 1984–1992 FE</td>
<td>8028</td>
</tr>
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</table>

<p>| | | | | | |</p>
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</tbody>
</table>

<table>
<thead>
<tr>
<th>Time effects</th>
<th>No</th>
<th>Yes</th>
<th>No</th>
<th>Yes</th>
</tr>
</thead>
<tbody>
<tr>
<td>Industry effects</td>
<td>No</td>
<td>No</td>
<td>Yes</td>
<td>Yes</td>
</tr>
</tbody>
</table>

Notes: Standard errors in parenthesis account for clustering at the industry and year level. Each column is from a separate regression of log weekly wages on the employment-weighted average log(equipment/labor) matched at the industry-year level. Additional controls include a quartic in age, marital status, non-white and sex dummies, years of education, year and industry dummies. The CPS sample includes full-time full-year workers aged 20–60 who earned more than 67$ a week in 1982 dollars. The DWS sample includes workers displaced from full-time jobs and is restricted to persons aged 20–60 who were employed at the time of the survey and worked at least 35 hours per week. Data on average equipment/labor ratios by industry-year are drawn from Compustat. Industries considered are durable and non-durable manufacturing, transport and utilities, wholesale trade, retail trade, other services.

### 3.3 Within Industry Dispersion of Wages and Capital Intensities

Equation 2 looks at the effect of average industry capital intensity on average wages but doesn’t take into account within industry dispersion in capital/labor ratios. To look at the effect of dispersion of within industry capital intensity on within industry wage dispersion I run the following regression:

\[
std(\log w)_{jt} = \alpha + \gamma std(\log \frac{k}{l})_{jt} + \varepsilon_{jt} \tag{3}
\]

\(std(\log \frac{k}{l})_{jt}\) is the employment-weighted log standard deviation of equipment/labor. This regression is weighted with weights proportional to the number of observations that are used to calculate \(std(\log \frac{k}{l})_{jt}\) in each industry-year cell.
Table 5 shows the results of estimation of equation 3 using March CPS and the DWS. The results that refer to the CPS, (table 5 row one and two), show that there is a positive association between capital intensity dispersion and wage dispersion within industries (column three). Wage and capital intensity dispersion are negatively associated across industry (column two). This indicates that the industries with the higher dispersion of wages are not the same as those with the higher dispersion of capital intensity. Column four however shows that within industry the growth of dispersion in capital intensity is associated with the growth of wage dispersion.

The same pattern is present in DWS data, however, the results appear to be weaker than those obtained on CPS data. Table 5 row three shows the results of estimation of equation 3 on the five DWS waves. The correlation between within industry dispersion of capital intensity and within industry dispersion of post-displacement wages is positive both across industries (column two) and within industries (column three). However the trend of within industry dispersion of wages is most explained by time dummies and it is only insignificantly positively associated with the concurrent increasing dispersion of capital intensity.

OLS estimates of the impact of within industry std.deviation of log equipment/labor ratio on within industry std.deviation of log earnings.

<table>
<thead>
<tr>
<th></th>
<th>Dependent variable: Std.deviation(log weekly earnings)</th>
<th>N obs.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.029*</td>
<td>(0.016)</td>
</tr>
<tr>
<td></td>
<td>-0.043*</td>
<td>(0.014)</td>
</tr>
<tr>
<td></td>
<td>0.113*</td>
<td>(0.041)</td>
</tr>
<tr>
<td></td>
<td>0.064*</td>
<td>(0.019)</td>
</tr>
<tr>
<td></td>
<td>CPS 1984–1992</td>
<td>54</td>
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<tr>
<td></td>
<td>-0.042*</td>
<td>(0.025)</td>
</tr>
<tr>
<td></td>
<td>-0.046*</td>
<td>(0.026)</td>
</tr>
<tr>
<td></td>
<td>0.098*</td>
<td>(0.028)</td>
</tr>
<tr>
<td></td>
<td>0.048*</td>
<td>(0.025)</td>
</tr>
<tr>
<td></td>
<td>DWS 1984–1992</td>
<td>30</td>
</tr>
<tr>
<td></td>
<td>0.196*</td>
<td>(0.052)</td>
</tr>
<tr>
<td></td>
<td>0.077*</td>
<td>(0.049)</td>
</tr>
<tr>
<td></td>
<td>0.479*</td>
<td>(0.142)</td>
</tr>
<tr>
<td></td>
<td>0.209</td>
<td>(0.164)</td>
</tr>
</tbody>
</table>

Notes: Regression weighted by the number of observations used to calculate the standard deviation of log(equipment/labor) in each year-industry cell. Each column is from a separate regression of standard deviation of log weekly wages on the employment-weighted standard deviation of log(equipment/labor) matched at industry-year level. The CPS sample includes full-time full-year workers aged 20–60 who earned more than 67% a week in 1982 dollars. The DWS sample includes workers displaced from full-time jobs and is restricted to persons aged 20–60 who were employed at the time of the survey and worked at least 35 hours per week. Data on standard deviation of log equipment/labor ratios by industry-year are drawn from Compustat. Industries considered are durable manufacturing, non-durable manufacturing, transport and utilities, wholesale trade, retail trade, other services.
4 A Theoretical Interpretation

This section gives an interpretation of the evidence presented earlier. According to that evidence, the increase in dispersion of capital intensity across firms is related to wage dispersion across workers.

In this section I present a model of residual wage inequality based on the increasing variance of firms’ capital intensities. Contrary to most previous models of residual wage inequality, this model is not based on the rising price of ex-ante differences in unobservable abilities. I suggest that the variance of the distribution of the demand of skills has increased over time. By the variance of the demand of skills I mean the variance of equipment capital investment across firms. Conversely the distribution of the supply of skills (i.e., unobserved ability across workers) has not become more disperse over time. In the next section I will review some of the existing evidence that supports both those hypothesis.

I build a search and matching model with identical workers and two types of firms. Firms differ in their optimal composition of equipment and structure. Firms sink their capital before searching for workers and the matching is random. As the relative price of equipment decreases over time, the dispersion of capital/labor ratios across firms increases. This force generates wage dispersion across identical workers as job changers and new entrants are matched to an increasing dispersed distribution of jobs.

The model is related to the literature on inter-industry wage differentials and in particular to the more recent theoretical developments that explain wage dispersion among equivalent workers with differences in firms’ technology. In many of those models firms are assumed to have differences in technology and wage dispersion is a consequence of technology dispersion. In Mortensen and Pissarides (1994) the differences in productivity across firms are due to firm or match specific shocks. In Acemoglu (2000) firms have different creation (capital) costs. My model is close to Acemoglu (2000). His model focuses on the effect of unemployment insurance and minimum wages on the composition of jobs. As in that model I assume that firms can have heterogeneous technologies but I focus on changes in their capital choices over time and the effect on wage inequality.

This paper is also linked to a recent literature that looks directly at the changes in the variance of the distribution of demand of skills. Acemoglu (1999) builds a model where the increase in the relative supply of skills changes firms’ investment decisions. When there are few skilled workers and the productivity gap between the skilled and unskilled is limited, firms create one type of job (one single level of $k$) and pool across all types of
workers. When the supply of skilled workers rises or their relative productivity increases, firms are induced to differentiate the types of jobs they offer. Some firms invest in more capital than others and target skilled workers only. That model, like mine, implies an increasing variance of equipment/labor ratios across firms. In that model the increasing dispersion of capital is due to the increase in the relative supply or the relative productivity of skills. In my model the increasing dispersion of capital is due to the decline in the relative price of equipment and to ex-ante technological differences across firms.

4.1 Changes in the Distribution of Demand and Supply of Skills

The increase over time in the average demand of skills has been advocated in numerous papers. The most popular reasons are skill biased technical change and trade with developing countries. However skill-biased technical change or organizational changes at the firm’s level may have also increased the variance of the demand of skills. The clearest exposition of this thesis is in Acemoglu (1999). In the same paper Acemoglu offers some evidence of the increased variance in the composition of jobs. Such evidence comes from different sources.

Changing recruitment practices of firms. Evidence of more selective practices and more accurate screening at recruitment level are interpreted as signs of a changing composition of jobs.

Better matching of firms and workers. Evidence from the PSID shows that more workers have the exact amount of education required for their job. There is less overeducation or undereducation and this is interpreted as evidence of better matching due to an increased variety of jobs offered.

Changes in the distribution of jobs. Constructing industry-occupation cells and ranking them according to their average wage, there is a shift of employment towards the lower and the higher ranking cells. This is interpreted as changing composition of jobs.

The distribution of on the job training has become more unequal. As on the job training is correlated with high wages and capital investment in the job, this evidence is interpreted as a more unequal distribution of capital investment.

---

6 Murnane and Levy [1996] and Cappelli and Wilk [1997].
7 Sicherman [1991].
8 Constantine and Neumark [1994].
Changes in capital/labor ratios. Caselli (1999) reports a sharp increase in the capital-labor ratio difference between the 90th and 10th most capital intensive industries. This evidence of more unequal distribution of capital-labor ratios across industries is interpreted as changing composition of jobs.

4.2 The Model

In this model there are identical workers and two types of firms. Firms differ in the composition equipment/structure investment. Firms rent a site and immediately upon renting a site, before meeting workers, decide how much equipment capital to install. Equipment capital is irreversible, i.e. when the relationship ends, it becomes obsolete. Equipment capital is optimized but structure capital is fixed. Both types of capital are sunk when the vacancy is opened, expenditure on structure is incurred immediately, expenditure on equipment only when the match takes place. The driving force of the increasing dispersion of equipment/labor ratios across firms is the decline in the price of equipment capital. As the cost of equipment capital decreases, ”good” firms that use a lot of equipment capital increase their optimal capital choice. This causes an increase in within wage inequality as workers are identical and the non competitive labor market implies that they receive a wage proportional to the equipment capital they are working with.

The economy is constituted of a mass $1$ of risk neutral workers and a larger mass of risk neutral firms. The technology of production is:

$$Y = (Y_b^\rho + \gamma Y_g^\rho)^{\frac{1}{\rho}}$$

where $Y_b$ and $Y_g$ are intermediate inputs. Since intermediate inputs are sold in competitive markets their prices are:

$$p_b = Y_b^\rho \gamma Y_g^\rho$$

Firms differ in the mix of equipment capital and structure capital. Good firms have a lot of equipment capital, bad firms have a lot of structure capital. Both types of firms can be inactive, vacant or filled. There is free entry of firms: at every point in time some inactive firms open a vacancy renting a site at price $c_g$ if it is a ”good” firm and $c_b$ if it is a ”bad” firm. After opening a vacancy and before meeting the workers, firms have to do their irreversible capital choices $k_g$ and $k_b$. The cost of installation are
incurred only at matching. Production takes place in the form of a match one firm-one worker. A worker matched with a firm with capital $k_j$ with $j = g, b$ produces:

$$y_j(k, l) = k_j^{\frac{1}{1-\alpha}}$$  (4)

In a search environment the matching is random. Workers have the probability $\phi$ of matching with a "good" firm and $(1 - \phi)$ of matching with a bad firm. $\phi = \frac{v_g}{v}$ is the proportion of vacant "good" firms among all vacancies. Vacant firms meet unemployed workers at the rate $q(\theta)$, unemployed workers meet vacant firms at the rate $\theta q(\theta)$ where $\theta = \frac{v}{u}$ is market tightness. Both firms and workers discount the future at rate $r$. Quits into unemployment to look for another job take place at rate $\lambda$. The rate of quits into unemployment is exogenous but it’s a good approximation of the empirical evidence that shows a stable number of job changers over time.

In a competitive labor market "good" jobs and "bad" jobs cannot coexist as workers are identical. In a search model since capital costs are sunk before workers are met, they remain idle until a match is formed. Good jobs will have to recover the bigger costs incurred at creation with higher flow profits. I solve the model in steady state only and I present the relevant Bellman equations. The discounted value of being unemployed is:

$$rU = \theta q(\theta)[\phi E(k_g) + (1 - \phi) E(k_b) - U]$$  (5)

An unemployed worker meets a good firm with probability $\theta q(\theta)\phi$ where $\theta q(\theta)$ is the flow probability of meeting a vacant firm and $\phi$ is the proportion of good firms among the vacancies. When the match takes place and both the worker and the firm accept the job, the worker gains $E(k_g)$ or $E(k_b)$ and he loses $U$. For simplicity I assume there are no unemployment benefits. The value of being employed in a good firm $E(k_g)$ is:

$$rE(k_g) = w(k_g) - \lambda(E(k_g) - U)$$  (6)

The value of being employed in a bad firm is:

$$rE(k_b) = w(k_b) - \lambda(E(k_b) - U)$$  (7)

where $w(k_j)$ is the wage rate for a worker in firm $j = g, b$ and $\lambda$ is the exogenous rate of quits. The value of a vacant firm $V(k_j)$ for $j = g, b$ is:
\[ rV(k_j) = q(\theta)[J(k_j) - Ck_j - V(k_j)] \]  

(8)

where \( q(\theta) \) is the flow probability of meeting an unemployed worker. When the match occurs and both the firm and the worker don’t turn it down, the firm gains the value of a filled firm \( J(k_j) \), incurs in the cost of capital \( Ck_j \) and it loses \( V(k_j) \). The value of a firm \( j = g, b \) matched with a worker is:

\[ rJ(k_j) = p_jk_j^{1-\alpha} - w(k_j) - \lambda[J(k_j) - V(k_j)] \]  

(9)

When jobs are destroyed at the exogenous rate \( \lambda \), firms exit the market. The zero profit condition for a firm \( j = g, b \) is:

\[ V(k_j) = c_j \]  

(10)

as the cost of renting a site is \( c_j \). Notice that good and bad firms face different rental costs \( c_j \). The crucial ingredient of this model, as described above, is that firms are different in their capital mix. The driving force of this model is the declining relative cost of equipment capital. The declining cost of equipment capital \( C \) favors good firms which have a high ratio equipment/structure and induces them to increase their capital choice \( k_g \). As soon as there are search frictions, there will be rents in the labor market. Rents will be split with Nash bargaining. Wages in good firms \( w(k_g) \) will be set such that:

\[ (1 - \beta)(E(k_g) - U) = \beta(J(k_g) - V(k_g)) \]  

(11)

in bad firms:

\[ (1 - \beta)(E(k_b) - U) = \beta(J(k_b) - V(k_b)) \]  

(12)

Equipment capital doesn’t appear in the sharing equation as it is sunk at the moment of bargaining and if the workers leave the relationship equipment capital has to be scrapped. Unemployment in steady state will be given by:

\[ u = \frac{\lambda}{\lambda + \theta q(\theta)} \]  

(13)
4.3 The Steady State Equilibrium

The equilibrium is given by capital choices \( k_g \) and \( k_b \), prices \( p_g \) and \( p_b \), unemployment rate \( u \), proportion of good firms \( \phi \) in the vacancy pool, market tightness \( \vartheta \) and wages \( w(k_g) \) and \( w(k_b) \) such that:

1) for all \( k_j : k_j = \operatorname{arg\,max}_{k_j} V(k_j') \) for \( j = g, b \).

2) for all \( k_j, k_j \) satisfies \( V(k_j) = c_j \) for \( j = g, b \).

3) all value functions \( J(k_j), V(k_j), U, E(k_j) \) are satisfied for \( j = g, b \).

4) \( u \) satisfies steady state equation

5) wages are given by 11 and 12

In equilibrium both good and bad jobs meet workers at the same rate and workers accept both types of vacancies. Therefore \( Y_b = (1 - u)\phi k_b^{1-\alpha} \) and \( Y_g = (1 - u)(1 - \phi)k_g^{1-\alpha} \). And prices are given by:

\[
p_g = ((1 - \phi)^\rho k_b^{(1-\alpha)\rho} + \gamma \phi^\rho k_g^{(1-\alpha)\rho})^{\frac{1-\rho}{\rho}} \gamma \phi^{\rho-1} k_g^{(1-\alpha)(\rho-1)} \quad (14)
\]

\[
p_b = ((1 - \phi)^\rho k_b^{(1-\alpha)\rho} + \gamma \phi^\rho k_g^{(1-\alpha)\rho})^{\frac{1-\rho}{\rho}} (1 - \phi)^\rho \phi^{-1} k_b^{(1-\alpha)(\rho-1)} \quad (15)
\]

Wages are set from 11, substituting 6, 9:

\[
w(k_j) = \beta(p_j k_j^{1-\alpha} - rc_j) + (1 - \beta) rU \quad (16)
\]

and from 11, 9 and 10

\[
rU = \theta q(\theta) \left[ \frac{\phi \beta}{1 - \beta} \left( \frac{rc_g}{q(\theta)} + Ck_g \right) + \frac{(1 - \phi) \beta}{1 - \beta} \left( \frac{rc_b}{q(\theta)} + Ck_b \right) \right] \quad (17)
\]

The optimal capacity \( k_j \) in equilibrium comes from \( V'(k_j) = 0 \) where \( V(k_j) \) is obtained using 8, 9 and 16. The two equations that determine capital choice when firms take both prices and wages for given are therefore:

\[
V'(k_g) = \frac{q(\theta)}{(r + \lambda)(r + q(\theta))} [p_g(1 - \alpha)k_g^{\alpha} - C] = 0 \quad (18)
\]

and

\[
V'(k_b) = \frac{q(\theta)}{(r + \lambda)(r + q(\theta))} [p_b(1 - \alpha)k_b^{\alpha} - C] = 0 \quad (19)
\]
In these two equations the first term indicates the marginal benefit of one more unit of capital while the second term indicates the marginal cost. The crucial result of the model comes from the two equations above. When the relative price of equipment capital $C$ falls, then equipment investment of good firms $k_g$ grows more than $k_b$. From the equations we obtain that $k_g > k_b$ as in equilibrium $p_g > p_b$ and $\frac{\delta(k_g-k_b)}{k_g} > 0$ as $k_g$ is more productive than $k_b$.

The equilibrium in the "good" job market and in the "bad" job market is given by the "job creation curve" $JC_j$ (which is obtained putting together equation 8, 9 and 10) and the wage equation 16 in each market. We have two locus, one where the "job creation curve" $JC_g$ meets the wage setting curve $w(k_g)$ (equation 16) of the "good" job market and the other where $JC_b$ meets $w(k_b)$. The two equilibrium loci that together with 18 and 19 (with 14 and 17 substituted in) define the equilibrium $\theta$ and $\phi$ are:

$$(1 - \beta)(p_jk_j^{1-\alpha} - rU) = \left[ \frac{r + q(\theta) + \lambda}{q(\theta)} \right] - \beta r]c_j + (r + \lambda)Ck_j$$

for $j = b, g$.

This model is particularly appealing as it gives a formula for within wage inequality that can be tested with the data used in the empirical part. Within wage inequality (using 16 and 20 for $j = b, g$) in this model is given by:

$$w(k_g) - w(k_b) = \frac{(r + \lambda)r(c_g-c_b)}{q(\theta)} + (r + \lambda)C(k_g-k_b)$$

(21)

Where the optimal capacity $k_j$ comes from $V_k(k_j) = 0$. Wage differences are related to the differences in capital investment but also to the job changing rate $\lambda$ and to the average duration of a vacancy $q(\theta)$.

4.4 Back of the Envelope Calculation

To have an idea of the importance of capital/labor ratios in increasing wage differentials I calibrate equation 21. Assume some values for the parameters of equation 21 over the period 1970-1992: interest rate $r = 0.06$, the job changing rate $\lambda = 0.2$. As an estimate of the matching function $q(\theta)$ for the US I take the values suggested in Blanchard and Diamond (1989): $q(\theta) = (\frac{u}{v})^\alpha$ with $\alpha = 0.4$. The unemployment to vacancy ratio $\frac{u}{v}$ is strongly anti-cyclical but on average during the period 1970-1992 $\frac{u}{v} = 2.5$. For $k_g - k_b$
I take the 90-10 differential in capital/labor ratios across firms calculated on Compustat data; this value increased by 12% over the period. Estimation of equation 21 indicates that within wage inequality \( w(k_g) - w(k_b) \) (90-10 differential of the residual distribution) has increased by roughly 15% point over the period 1970-1992 due to the increasing dispersion of capital/labor ratios across firms. According to Juhn, Murphy and Pierce the 90-10 differential of within group wage inequality increased by 30 percentage points from 1970 to 1992 in the US. This means that the mechanism that acts through the increasing dispersion of firms’ capital/labor ratios can account for 1/2 of the total increase in within group wage inequality.

A caveat about this rough estimation is the fact that the results are very sensitive to the assumptions about reversibility of capital. If capital is assumed to be reversible like in Acemoglu (2000) within wage inequality is given by:

\[
    w(k_g) - w(k_b) = \frac{(r + \lambda)r(k_g - k_b)}{q(\theta)}
\]

where now \( k_j \) is total capital i.e. equipment and structure. If I estimate this equation the increase in dispersion of capital/labor ratios can explain only 1/30 of the total increase in wage inequality. The main difference is due to the fact that when capital is irreversible, wages appropriate not only part of the flow cost of capital but part of the full sunk investment.

### 5 Conclusions

In this paper I document the increasing cross-firm dispersion of equipment capital/labor ratios in the US labor market using Compustat data. The increase takes place both between and within industries.

I match Compustat data on equipment capital intensity to CPS and DWS data on individual wages at the industry-year level. A 1% percent increase in average industry capital intensity is associated to a 0.11% increase in the average weekly wage in the CPS, to a 0.13% increase in the Displaced Workers Survey. More importantly for the scope of this paper the increase of the variance in capital/labor ratios across firms appears to be also positively related to the increasing variance of wages across workers. The correlation holds within industries even after controlling for time effects.

To explain these empirical regularities I adopt a search and matching model where identical workers are matched to two types of firms. Firms
differ in their optimal composition of capital between equipment and structure. As the relative price of equipment falls over time, the distribution of capital/labor ratios becomes more dispersed across firms and job changers face an increasingly wide variety of jobs. Residual wage inequality increases as identical workers are randomly matched to an increasingly dispersed distribution of capital/labor ratios.

Simple calibration of the model indicates that the dispersion of capital/labor ratios can explain up to one half of the total increase in within group wage inequality.

References


